

Topics for Exam 2

1. Consequences of Completeness

- 1.1. Archimedean Property
- 1.2. Density of the rational numbers in the set of real numbers.

2. Sequences of Real Numbers

- 2.1. Definition of convergence and limit of a sequence
- 2.2. The squeeze theorem for sequences
- 2.3. Bounded, monotone convergence theorem
- 2.4. Subsequences
- 2.5. Cauchy sequences

Relevant sections and chapters in the text: Section 4.6, Chapter 5, Section 6.1 and Sections 9.2-9.5.

Relevant problem sets: 4 and 5.

Relevant assignments: 7 through 12.

Important Concepts

Completeness, denseness of rational numbers, convergence, Cauchy criterion, monotone and bounded sequences.

Important Results.

1. \mathbf{Q} is dense in \mathbf{R} : Problem 5 in Problem Set #4
2. The Squeeze theorem for sequences: Problem 2 in Problem Set #5
3. Bounded, monotone convergence theorem: Problem 7 in Problem Set #5

Important Skills

1. Know how to prove whether a given sequence converges.
2. Know how to apply the Squeeze Theorem for sequences.
3. Know how to apply the bounded, monotone convergence theorem.