

Topics for Final Exam**1. Probability Spaces**

- 1.1 Sample spaces
- 1.2 σ -Fields
- 1.3 Probability functions
- 1.4 Independent events
- 1.5 Conditional probability

2. Random Variables

- 2.1 Continuous and discrete random variables
- 2.2 Cumulative distribution function (cdf)
- 2.3 Probability density function (pdf) and probability mass function (pmf)

3. Expectations of Random Variables

- 3.1 Expected Value a random variable
- 3.2 Expected value of functions of random variables
- 3.3 Moments and moment generating function
- 3.4 Variance of a random variable

4. Joint Distributions

- 4.1 Joint distribution of two random variables
- 4.2 Marginal distributions
- 4.3 Independent random variables

5. Special Distributions

- 5.1 Discrete distributions: Bernoulli, Binomial, Geometric, Hypergeometric, (Discrete) Uniform and Poisson.
- 5.2 Continuous distributions: Uniform, Exponential, Normal and Chi-Squared.

6. Limiting Distributions

- 6.1 The Poisson distribution as a limit of binomial distributions.
- 6.2 Convergence in distribution
- 6.3 mgf Convergence Theorem

7. Limit Theorems

- 7.1 Chebyshev Inequality
- 7.2 Convergence in probability
- 7.3 The Law of Large Numbers
- 7.4 Random samples: Sample Mean and Sample Variance
- 7.5 The Central Limit Theorem
- 7.6 Applications of the Central Limit Theorem: Point Estimates and Confidence Intervals.

Relevant sections in the text: 1.4, 1.5, 1.6, 2.1, 2.2, 2.3, 3.1, 3.2, 3.4, 3.5, 4.1, 4.2, 4.3, 5.4, 5.6, 5.7, 6.2, 6.3, 8.2, 8.3 and 8.5

Important Concepts

Sample space, σ -Field, probability function, probability space, random variable, continuous and discrete random variables, cumulative distribution function (cdf), probability mass function (pmf), and probability density function (pdf), expectation, moments, moment generating function (mgf), variance, joint distributions, marginal distributions, independent random variable, convergence in distribution, convergence in probability, limiting distribution.

Important Skills

1. Know how to compute probabilities of events
2. Know how to compute the cdf and the pdf (or pmf) of a random variable
3. Know how to compute expectations, moments, variance and moment generating functions.
4. Know how to compute the joint cdf and the joint pdf (or pmf) of two or more random variables

5. Know how to compute marginal distributions
6. Know how to compute probabilities based on joint distributions
7. Know how to use independence
8. Know how to apply the mgf convergence theorem
9. Know how to apply the central limit theorem.