FORMAL MODEL & NOTATION:

$$\left. \begin{array}{l} Y_{11}, Y_{12}, \ldots Y_{1n_1} \text{ are a SRS of size } n_1 \text{ from } N(\mu_1, \sigma^2) \text{ distribution} \\ Y_{21}, Y_{22}, \ldots Y_{2n_2} \text{ are a SRS of size } n_2 \text{ from } N(\mu_2, \sigma^2) \text{ distribution} \\ \vdots \\ Y_{r1}, Y_{r2}, \ldots Y_{rn_r} \text{ are a SRS of size } n_r \text{ from } N(\mu_r, \sigma^2) \text{ distribution} \end{array} \right\} = \left\{ \begin{array}{l} Y_{ij} \sim N(\mu_i, \sigma^2) \\ Y_{ij} = \mu_i + \epsilon_{ij} \\ \epsilon_{ij} \sim N(0, \sigma^2) \end{array} \right.$$

ESTIMATION

The value of μ_i that minimizes: $\sum_{i=1}^r \sum_{j=1}^{n_i} (Y_{ij} - \mu_i)^2$ is the least squares estimate of μ_i . That is, $\hat{\mu}_i = \overline{Y}_i$.

Residual sum of squares (within sum of squares) = SSE = $\sum_{i=1}^{r} \sum_{j=1}^{n_i} (Y_{ij} - \overline{Y}_{i.})^2$

THEORY

Variable		Distribution	Assumptions
•	~ ~		CLT, normal pop, $= \sigma_i^2$ normal pop, $= \sigma_i^2$ normal pop, $= \sigma_i^2$, under H_o normal pop, $= \sigma_i^2$, under H_o
			$E(MSE) = \sigma^2$ $E(MSTR) = \sigma^2 + \sum_{i=1}^{r} \frac{n_i(\mu_i - \mu_i)^2}{(r-1)}$

F-distribution:

If, in fact, H_0 is true (that is, $\mu_1 = \mu_2 = \ldots = \mu_r$), then we know our sums of squares are independent χ^2 random variables. Therefore:

$$F\text{-stat} = \frac{MSTR}{MSE} \sim F_{(r-1,n_T-r)}$$

Note: if H_0 is not true, then MSTR will be too big and the distribution of F-stat will shift to the right of $F_{(r-1,n_T-r)}$.