

Assignment #12

Due on Monday, November 16, 2009

Read Section 3.1 on *The Calculus of Curves*, pp. 53–65, in Bressoud.

Read Section 5.2 on *Line Integrals*, pp. 113–119, in Bressoud.

Do the following problems

1. Consider a portion of a helix, C , parametrized by the path

$$\sigma(t) = (\cos t, t, \sin t) \quad \text{for } 0 \leq t \leq \pi.$$

Let $f(x, y, z) = x^2 + y^2 + z^2$ for all $(x, y, z) \in \mathbb{R}^3$. Evaluate $\int_C f$.

2. Let $f(x, y) = y$ for all $(x, y) \in \mathbb{R}^2$. For each of the following curves, C , in the plane, evaluate $\int_C f$.

- (a) C is the segment along the x axis from $(0, 0)$ to $(1, 0)$.
- (b) C is the segment along the y axis from $(0, 0)$ to $(0, 1)$.
- (c) C is the unit circle in \mathbb{R}^2 .

3. Exercise 10 on page 120 in the text.

4. Exercise 12 on page 120 in the text.

5. Let f be a real valued function which is C^1 in an open interval containing the closed and bounded interval $[a, b]$. Define C to be the portion of the graph of f over $[a, b]$; that is,

$$C = \{(x, y) \in \mathbb{R}^2 \mid y = f(x), a \leq x \leq b\}.$$

- (a) Give a parametrization for C and compute the arc length, $\ell(C)$, of C .
- (b) Compute the arc length along the graph of $y = \ln x$ from $x = 1$ to $x = 2$.
Note: In order to do part (b), you'll need to remember, or review, everything you learned about evaluating integrals in your single variable Calculus courses.