# Department of Mathematics Pomona College

### Math 152. Statistical Theory Fall 2009

#### **Course Outline**

| Time and Place:      | MWF 9:00 am - 9:50 am Millikan 218                            |  |  |  |  |
|----------------------|---|--|--|--|--|
| Instructor:          | Dr. Adolfo J. Rumbos  |  |  |  |  |
| Office:              | Andrew 259  |  |  |  |  |
| Phone/e-mail:        | ext. 18713 / arumbos@pomona.edu                               |  |  |  |  |
| <b>Office Hours:</b> | MWF $10:00 \text{ am} - 11:00 \text{ am}$ ; or by appointment |  |  |  |  |
| Text:                | Introduction to Mathematical Statistics, Sixth Edition        |  |  |  |  |
|                      | by Robert V. Hogg, Joseph W. McKean and Allen T. Craig.       |  |  |  |  |
| Course Website:      | http://pages.pomona.edu/~ajr04747/                            |  |  |  |  |
| Prerequisites:       | Probability (Math 151 PO or equivalent course)                |  |  |  |  |

**Course Description.** This is a course in *statistical inference*. Loosely speaking, statistical inference is the process of going from information gained from a sample to inferences about a population from which the sample is taken. There are two aspects of statistical inference that we'll be studying in this course: estimation and hypothesis testing. In estimation, we try to determine *parameters* from a population based on quantities, referred to as *statistics*, calculated from data in a sample. The degree to which the estimates resemble the parameters being estimated can be measured by ascertaining the probability that a certain range of values around the estimate will contain the actual parameter. The use of probability is at the core of statistical inference; it involves the postulation of a certain probability model underlying the situation being studied and calculations based on that model. The same procedure can in turn be used to determine the degree to which the data in the sample support the underlying model; this is the essence of hypothesis testing. A solid knowledge of probability is therefore essential for understanding statistical inference.

The course topics are listed in the attached tentative schedule of lectures and examinations.

**Assigned Readings and Problems.** Readings and problem sets will be assigned at every lecture and collected on an alternate basis. Students are strongly encouraged to work on every assigned problem. Late homework assignments will not be graded.

**Grading Policy.** Grades will be based on the homework, three 50-minute examinations, plus a comprehensive final examination. The overall score will be computed as follows:

| homework              | 20% |
|-----------------------|-----|
| three 50-minute exams | 50% |
| final examination     | 30% |

#### **Final Examination.**

Time: Thursday, December 17, 2009 9:00 am - 11:00 am. Place: Millikan 218

## Math 152. Statistical Theory

### Fall 2009

### **Tentative Schedule of Lectures and Examinations**

| Date   |            |        | Торіс   |
|--------|------------|--------|---|
| W<br>F | Sep<br>Sep | 2<br>4 | Introduction: A problem from statistical inference Sampling |
| М      | Sep        | 7      | Sampling (continued)  |
| W      | Sep        | 9      | Estimating the mean   |
| F      | Sep        | 11     | Estimating the mean (continued)                             |
| М      | Sep        | 14     | Approximate interval estimates                              |
| W      | Sep        | 16     | Interval estimates (continued)                              |
| F      | Sep        | 18     | The $\chi^2$ and t-distributions                            |
| М      | Sep        | 21     | Goodness of fit   |
| W      | Sep        | 23     | Introduction to hypothesis testing                          |
| F      | Sep        | 25     | Hypothesis tests (continued)                                |
| М      | Sep        | 28     | Review  |
| W      | Sep        | 30     | Exam 1  |
| F      | Oct        | 2      | Maximum likelihood estimation                               |
| М      | Oct        | 5      | Maximum likelihood estimation (continued)                   |
| W      | Oct        | 7      | Efficiency  |
| F      | Oct        | 9      | Rao-Cramer lower bound                                      |
| Μ      | Oct        | 12     | Maximum likelihood tests                                    |
| W      | Oct        | 14     | Maximum likelihood tests (continued)                        |
| F      | Oct        | 16     | Sufficiency   |
| М      | Oct        | 19     | Fall Recess   |
| W      | Oct        | 21     | Sufficiency (continued)                                     |
| F      | Oct        | 23     | Completeness and independence                               |
| М      | Oct        | 26     | Completeness and independence (continued)                   |
| W      | Oct        | 28     | Review  |
| F      | Oct        | 30     | Exam 2  |
| М      | Nov        | 2      | Power of hypothesis tests                                   |
| W      | Nov        | 4      | Power of hypothesis tests (continued)                       |
| F      | Nov        | 6      | The Neyman-Pierson lemma                                    |

| Date |     |    | Торіс                              |
|------|-----|----|------------------------------------|
| М    | Nov | 9  | Interval estimates (revisited)     |
| W    | Nov | 11 | Likelihood ratio tests             |
| F    | Nov | 13 | Likelihood ratio tests (continued) |
| М    | Nov | 16 | Introduction to Bayesian inference |
| W    | Nov | 18 | Bayesian procedures                |
| F    | Nov | 20 | Bayesian procedures (continued)    |
| М    | Nov | 23 | Bayesian procedures (continued)    |
| W    | Nov | 25 | Problems                           |
| F    | Nov | 27 | Thanksgiving Recess                |
| М    | Nov | 30 | Problems                           |
| W    | Dec | 2  | Review                             |
| F    | Dec | 4  | Exam 3                             |
| М    | Dec | 7  | Review                             |
| W    | Dec | 9  | Review                             |
|      |     |    |                                    |

Tu Dec 17 Final Examination