

**Topics for Final Exam****1. The Fundamental Theorem of Calculus**

1.1 Solving the initial value problem  $\begin{cases} \frac{dy}{dt} = f(t) \\ y(t_0) = y_0, \end{cases}$  where  $f$  is a continuous function defined on an interval containing  $t_0$ .

1.2 Evaluating integrals: Changing variables.

**2. The Natural Logarithm and Exponential Functions**

2.1 Solving first order differential equations.

2.2 Separation of variables.

**3. Solving First Order Linear Differential Equations**

3.1 Method of Integrating Factor.

3.2 Integration by parts.

**4. Solving the Non-Linear, First-Order Differential Equation**

4.1 Existence and Uniqueness.

4.2 Partial Fractions.

**5. Linear Approximations**

5.1 Linear approximation to a differentiable function.

5.2 Error in the linear approximation.

**6. Qualitative Analysis of First Order Equations**

6.1 Isolated equilibrium points; stability and asymptotic stability; unstable equilibrium point.

6.2 Existence and uniqueness; global existence and long-term behavior.

6.3 Principle of Linearized Stability

**7. Applications to Modeling**

7.1 Conservation principles.

7.2 One compartment Models.

7.3 Analysis of population models for single species.

**Relevant Sections in the Text and Class Lecture Notes:**

Sections 4.24, 4.4, 4.2, 4.3, 4.5, 4.6, 5.2 and 5.1 in the text; Chapters 2, 3, 4 and 5 in the class lecture notes.

**Relevant Assignments:** 1–19.

**Important Concepts:** Differential equation, initial value problem, conservation principle, linear approximation, linearized equation, equilibrium point, stability.

**Important Skills:** Know how to apply the conservation principle to derive differential equation models; know how to use separation of variables to solve first order differential equations; know how to obtain qualitative information about solutions to first order differential equations; know how to integrate by parts; know how to use partial fractions; know how to use linear approximations to differentiable functions; know how to estimate the error in the linear approximation; know how to apply the principle of linearized stability.