# Department of Mathematics <br> Pomona College 

Course Outline<br>Math 101. Introduction to Analysis

Fall 2012

| Time and Place: | MWF 10:00 am - 10:50 am, Millikan 218 |
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| Instructor: | Dr. Adolfo J. Rumbos |
| Office: | Andrew 259 |
| Phone/e-mail: | ext. 18713 / arumbos@pomona.edu |
| Office Hours: | MWF 8:45 am - 9:45 am, or by appointment |
| Text: | Introduction to Real Analysis by Michael J. Schramm; Dover |
| Course Website | http://pages.pomona.edu/~ajr04747/ |
| Prerequisite: | Linear Algebra |

Course Description. The main goal of this course is to give a rigorous treatment to the study of continuity of real valued functions of a single real variable. This will require an in-depth study of the real numbers system and its properties since many important facts about continuous functions (eg., the intermediate-value theorem) would not be valid without some of those properties.

About two thirds of the class time will be spent on student presentations. The instructor will lecture or lead discussion the other third of the time. The content of the course is dictated by a series of assigned problems, most of which will involve the development of mathematical arguments, which will be presented by the students to the class. In addition, students will be required to give a formal presentation at the end of the semester on a special topic related to the course material (see attached list of special topics).

Assigned Readings and Problem Sets. Readings and problem sets will be assigned at every class meeting. Students are expected to do all the assigned reading and work on all the assigned problems, as they will be asked to present solutions to the class at a subsequent meeting. Each student will be required to keep a journal in which complete solutions of all problems presented in class are recorded. This journal is to be separate from notebooks in which the student takes notes during lectures and student presentations.

Grading Policy. Grades will be based on presentations and solutions to assigned problems, two 50-minute examinations, weekly assignments, and a formal presentation. The overall score will be computed as follows:

| Problem solutions journal | $15 \%$ |
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| Homework assignments | $20 \%$ |
| Problem solutions presentation | $10 \%$ |
| Two examinations | $40 \%$ |
| Formal presentation | $15 \%$ |

# Tentative Schedule of Topics, Presentations and Examinations 

| Date |  | Topic |
| :---: | :---: | :---: |
| W | Sep 5 | Introduction to mathematical reasoning |
| F | Sep 7 | Ways of proving mathematical statements |
| M | Sep 10 | Propositional logic |
| W | Sep 12 | The natural numbers and the principle of induction |
| F | Sep 14 | Divisibility |
| M | Sep 17 | The real numbers system. Numbers: rational and irrational |
| W | Sep 19 | Properties of real numbers |
| F | Sep 21 | Properties of real numbers (continued) |
| M | Sep 24 | Properties of real numbers (continued) |
| W | Sep 26 | Order in the set of real numbers |
| F | Sep 28 | Order in the set of real numbers (continued) |
| M | Oct 1 | Completeness |
| W | Oct 3 | Consequences of completeness |
| F | Oct 5 | Consequences of completeness (continued) |
| M | Oct 8 | Topology of the real line |
| W | Oct 10 | Review |
| F | Oct 12 | Exam 1 |
| M | Oct 15 | Sequences of real numbers |
| W | Oct 17 | Convergence |
| F | Oct 19 | Monotone sequences |
| M | Oct 22 | Fall Recess |
| W | Oct 24 | Bounded sequences |
| F | Oct 26 | Cauchy sequences and convergence |
| M | Oct 29 | Continuous functions |
| W | Oct 31 | Properties of continuous functions |
| F | Nov 2 | Properties of continuous functions (continued) |
| M | Nov 5 | The intermediate value theorem |
| W | Nov 7 | The extremal value theorem |
| F | Nov 9 | The extremal value theorem (continued) |
| M | Nov 12 | Problems |
| W | Nov 14 | Review |
| F | Nov 16 | Exam 2 |


| Date |  |  |
| :--- | :--- | ---: |
| M | Nov | 19 |
| W | Nov | 21 |
| F | Nov | 23 |
| M | Nov | 26 |
| W | Nov | 28 |
| F | Nov | 30 |
| M | Dec | 3 |
| W | Dec | 5 |
| F | Dec | 7 |
| M | Dec | 10 |
| W | Dec | 12 |

## Topic

Special Topic
Special Topic
Thanksgiving Recess
Special Topic
Special Topic
Special Topic
Special Topic
Special Topic
Special Topic
Special Topic
Special Topic

