

## Exam 1 (Part I)

Friday, October 3, 2014

Name: \_\_\_\_\_

This is the in-class portion of Exam 1. This is a closed-book and closed-notes exam.

Show all significant work and give reasons for all your answers. Use your own paper and/or the paper provided by the instructor. You have up to 40 minutes to work on the following 2 questions. Relax.

1. Let  $(\mathcal{C}, \mathcal{B}, \Pr)$  denote a probability space, and let  $A$  and  $B$  denote events in  $\mathcal{B}$ .
  - (a) State what it means for  $A$  and  $B$  to be independent.
  - (b) State what it means for  $A$  and  $B$  to be mutually exclusive.
  - (c) Assume that  $\Pr(B) > 0$ . Define the conditional probability of  $A$  given  $B$ .
  - (d) Given that  $\Pr(B) > 0$ , state the multiplication rule for computing the probability of the joint occurrence of  $A$  and  $B$ .
  - (e) State the inclusion-exclusion principle for computing  $\Pr(A \cup B)$ .
  
2. An experiment consists of flipping a fair coin three consecutive times.
  - (a) List all the elements of the sample space,  $\mathcal{C}$ , for this experiment.
  - (b) For each element,  $c$ , of the sample space,  $\mathcal{C}$ , let  $N_H(c)$  denote the number of heads in  $c$ , and  $N_T(c)$  the number of tails in  $c$ . Put

$$X(c) = N_H(c) - N_T(c), \quad \text{for all } c \in \mathcal{C}.$$

List all possible values for the random variable  $X$ .

- (c) Compute the probability mass function (pmf) for  $X$ . Explain the reasoning behind your calculations.
- (d) Compute  $\Pr(X \leq 0)$ . Explain the reasoning behind your calculations.