## Assignment #1

## Due on Wednesday, September 11, 2013

Read Chapter 1, An Example from Statistical Inference, in the class lecture notes at http://pages.pomona.edu/~ajr04747/

**Read** Section 1.4 on *Set Theory* in DeGroot and Schervish.

**Do** the following problems

- 1. Let  $\mathcal{C}$  denote a sample space and A be a subset of  $\mathcal{C}$ . Establish the following set theoretic identities:
  - (a)  $A \cap \emptyset = \emptyset$ ,
  - (b)  $A \cup \emptyset = A$ ;

where  $\emptyset$  denotes the empty set. Justify your steps.

- 2. Let  $\mathcal{C}$  denote a sample space and A and B denote subsets of  $\mathcal{C}$ . Establish the following set theoretic identities:
  - (a)  $(A^c)^c = A$ ,
  - (b)  $(A \cup B)^c = A^c \cap B^c$ ;

where  $A^c$  denote the complement of A.

- 3. Let  $\mathcal{C}$  denote a sample space and A, B and C denote subsets of  $\mathcal{C}$ . Prove the following distributive properties:
  - (a)  $A \cap (B \cup C) = (A \cap B) \cup (A \cap C)$
  - (b)  $A \cup (B \cap C) = (A \cup B) \cap (A \cup C)$
- 4. Let A and B be subsets of the sample space C. The set difference  $A \setminus B$  is defined to be

$$A \backslash B = \{ x \in A \mid x \not\in B \};$$

thus,  $A \setminus B$  is a subset of A that contains those elements in A which are not in B.

Prove that

- (a)  $A \setminus B = A \cap B^c$ ,
- (b)  $B \setminus (A \cap B) = A^c \cap B$
- 5. Suppose that  $A \subseteq B$ . Prove that  $B^c \subseteq A^c$ .