Assignment #12

Due on Wednesday, October 23, 2013

Read Chapter 4 on *Expectation of Random Variables* in the class lecture notes at http://pages.pomona.edu/~ajr04747/

Read Section 4.2 on *Properties of Expectations* in DeGroot and Schervish.

Do the following problems

- 1. A balanced die is tossed n times. Let X denote the number of 1's that come up. Give the pmf for X and compute its expectation.
- 2. Let X and Y denote independent Binomial(n, p) random variables and put Z = X + Y. Determine the pmf of Z and compute its expectation.

Hint: Suppose there are n red balls and n blue balls in a box. Compute the number of ways of picking k balls out of the box, l of which are red and k - l of which are blue.

- 3. (Random Walk on the Integers). A particle starts at x = 0 and, after one unit of time, it moves one unit to the right with probability p, for 0 , or tothe left with probability <math>1 - p. Let X_1 denote the position of the particle after one unit of time and X_2 denote that after 2 units of time. Give the probability mass functions for X_1 and X_2 and compute their expectations. Assume that at each time step, whether a particle will move to the right or to the left is independent of where it has been.
- 4. (Random Walk on the Integers, Continued). Let X_3 denote the position of the particle in the previous problem after 3 units of time. Give its pmf and expectation. Generalize this result to X_n , the position of the particle after n units of time.
- 5. Toss a coin 100 times, and let X denote the number of heads that come up. Given that the probability of a head is p, where $0 , give the distribution function of X and compute <math>Pr(35 \le X \le 45)$ for the cases p = 0.5 and p = 0.4.