Assignment #18

Due on Wednesday, November 5, 2014

Read Section 6.2 on *The Poisson Distribution* in the class lecture notes at http://pages.pomona.edu/~ajr04747/

Read Section 5.4 on The Poisson Distribution in DeGroot and Schervish.

Do the following problems

1. We have seen in the lecture that if X has a Poisson distribution with parameter $\lambda > 0$, then it has the pmf:

$$p_{X}(k) = \frac{\lambda^{k}}{k!} e^{-\lambda}$$
 for $k = 0, 1, 2, 3, ...;$ zero elsewhere.

Use the fact that the power series $\sum_{m=0}^{\infty} \frac{x^m}{m!}$ converges to e^x for all real values of x to compute the mgf of X.

Use the mgf of X to determine the mean and variance of X.

2. Let X_1, X_2, \ldots, X_m be independent random variables satisfying $X_i \sim \text{Poisson}(\lambda)$ for all $i = 1, 2, \ldots, m$ and some $\lambda > 0$. Define

$$Y = X_1 + X_2 + \dots + X_m.$$

Determine the distribution of Y; that is, compute its pmf.

- 3. Suppose that on a given weekend the number of accidents at a certain intersection has a Poisson distribution with mean 0.7. What is the probability that there will be at least three accidents in the intersection during the weekend?
- 4. Suppose that a certain type of magnetic tape contains, on average, three defects per 1000 feet. What is the probability that a roll of tape 1200 feet long contains no defects?
- 5. Let X_1 and X_2 be independent random variables and that X_i has a Poisson distribution with mean λ_i (i = 1, 2). For a fixed value of k (k = 0, 1, 2, 3, ...), determine the conditional distribution of X_1 given that $X_1 + X_2 = k$.