### Topics for Exam 1

## 1. Vector Space Structure in Euclidean Space

- 1.1 Definition of *n*–Dimensional Euclidean Space
- 1.2 Vector addition and scalar multiplication
- 1.3 Spans
- 1.4 Linear independence

# 2. Subspaces of Euclidean Space

- 2.1 Bases
- 2.2 Dimension
- 2.3 Coordinates

#### 3. Connections with the Theory of Linear Equations

- 3.1 Homogeneous systems
- 3.2 Fundamental Theorem for homogenous systems of linear equations
- 3.3 Nonhomogeneous systems

Relevant sections in text: 1.1, 1.2, 1.3, 1.4, 1.5 and 1.6.

Relevant sections in the online class notes: 2.1, 2.2, 2.3, 2.4, 2.5, 2.6, 2.7, 2.8, 2.9, 2.10 and 2.11.

**Relevant assignments**: 1, 2, 3, 4, 5, 6, 7, 8, 9, 10 and 11.

**Important concepts**: Euclidean space, linear independence, span, subspaces, bases, dimension and coordinates.

Important skills: Know how to determine whether subsets of  $\mathbb{R}^n$  are linearly independent; know how to tell whether a given subset of  $\mathbb{R}^n$  is a subspace; know how to tell whether a set of vectors in  $\mathbb{R}^n$  spans a subspace; know how to compute the span of a set of vectors; know how to solve systems of linear equations; know how to determine bases for subspaces of Euclidean space; know how to compute dimensions of subspaces; know how to find coordinates of vectors relative to ordered bases.