## Exam 2 (Part II)

Monday, April 5, 2010
Name: $\qquad$
This is the out-of-class portion of Exam 2. There is no time limit for working on the following problem. This is a closed-book exam; you are only allowed to consult the distributions sheet that was handed out in class previously. You are not allowed to consult your notes or with anyone.
Show all significant work and justify all your answers. Write your name on this page and staple it to your solutions.

## Due on Wednesday, April 7, 2010

3. Luria and Delbrück ${ }^{1}$ devised the following procedure (known as a fluctuation test) to estimate the mutation rate, $a$, for certain bacteria:
Imagine that you start with a single normal bacterium (with no mutations) and allow it to grow to produce several bacteria. Place each of these bacteria in test-tubes each with media conducive to growth. Suppose the bacteria in the test-tubes are allowed to reproduce for $n$ division cycles. After the $n^{\text {th }}$ division cycle, the content of each test-tube is placed onto a agar plate containing a virus population which is lethal to the bacteria which have not developed resistance. Those bacteria which have mutated into resistant strains will continue to replicate, while those that are sensitive to the virus will die. After certain time, the resistant bacteria will develop visible colonies on the plates. The number of these colonies will then correspond to the number of resistant cells in each test tube at the time they were exposed to the virus.
(a) Let Let $M(t)$ denote the number of bacteria that develop a mutation to resistant strains during the time interval $[0, t]$. Make an assumption regarding the distribution of the random variable $M(t)$ and use that assumption to compute

$$
P[M(t)=0],
$$

the probability that there will be no mutations to resistance in the time interval $[0, t]$.
(b) Estimate the probability, $p_{o}$, that at the end of the $n$ division cycles there will be no resistant bacteria. State all assumptions you make and justify your answer.

[^0](c) Use the formula for $P[M(t)=0]$ that you obtained in part (a), together with the estimate for $p_{o}$ that you obtained in part (b), to estimate, $\mu(t)$, the average number of mutations leading to resistant bacteria in the time interval $[0, t]$, where $t$ corresponds to $n$ division cycles. Explain how you may use the estimate for $\mu(t)$ to estimate the mutation rate, $a$.
(d) Table 1 shows data from an experiment performed by Luria and Delbrück involving 12 similar cultures of about $5 \times 10^{8}$ bacteria each. The first column shows the number-label of the cultures, and the second column shows the number of resistant bacteria in each culture.

Table 1: Luria and Delbrück Experiment No. 17

| Culture No. <br> Label | Resistant <br> Bacteria |
| :---: | :---: |
| 1 | 1 |
| 2 | 0 |
| 3 | 0 |
| 4 | 7 |
| 5 | 0 |
| 6 | 303 |
| 7 | 0 |
| 8 | 0 |
| 9 | 3 |
| 10 | 48 |
| 11 | 1 |
| 12 | 4 |

Use the data in Table 1 and your results in part (c) to estimate:
i. The average number of mutations, $\mu$, that occurred before the bacteria were exposed to the virus;
ii. The mutation rate, $a$; that is, the probability that a given bacterium will mutate in a division cycle.


[^0]:    ${ }^{1}$ (1943) Mutations of bacteria from virus sensitivity to virus resistance. Genetics, 28, 491-511

