## Topics for Exam 1

## 1. Euclidean Space

- 1.1 Definition of *n*–Dimensional Euclidean Space
- 1.2 Spans, Lines and Planes
- 1.3 Dot Product and Euclidean Norm
- 1.4 Orthogonality and Projections
- 1.5 The Cross Product in  $\mathbb{R}^3$

## 2. Continuous Functions

- 2.1 Vector fields, scalar fields and paths
- 2.2 Definition of continuous function
- 2.3 Compositions of Continuous Functions
- 2.4 Limits and continuity

## 3. Differentiability

- 3.1 Definition of differentiability
- 3.2 The derivative as a linear approximation
- 3.3 Derivatives of vector valued functions
- 3.4 Derivatives of scalar fields
  - i. The gradient
  - ii. Partial derivatives
  - iii. Directional derivatives

Relevant sections in the text: Sections 1.2, 2.1, 2.3, 2.5, 3.3, 4.1, 4.2, 4.3

Relevant chapters in the online class notes: Chapters 2, 3 and 4.

**Important Concepts**: Euclidean space, dot product, orthogonal projections, cross product, continuous function, differentiability, the derivative map, partial derivatives, and the gradient.

**Important Skills**: Know how to compute projections; know how to find equations of lines and planes; know how to show that a function is continuous or not; know how to show whether a function is differentiable or not; know how to compute partial derivatives, gradients and directional derivative of scalar fields.