

Rules of Logarithms

1. Rewrite the following expressions as logarithms of one quantity with coefficient 1.

(a) $\frac{1}{2} \ln x + \ln 5$

(b) $\log_2 x + 4 \log_2(x + 1) - \frac{1}{3} \log_2(x - 1)$

(c) $5 \ln x + 2 \ln 3 - 3 \ln \left(\frac{1}{y} \right)$

2. Use the rules of logarithms to expand the following expressions so that there are no logarithms of products, quotients, or powers.

(a) $\ln \sqrt[3]{x^3 y}$

(b) $\log_{10} \frac{10}{4x^2}$

(c) $\ln \left(\frac{x\sqrt{y}}{(1+x)^3} \right)$

3. Suppose $\ln(x) = 2$, $\ln(y) = 3$, and $\ln(z) = 6$. Evaluate the following expressions.

(a) $\ln(xyz)$

(b) $\ln(x^2y)$

(c) $\ln\left(\frac{x^3}{\sqrt{z}}\right)$