

Score: \_\_\_\_\_

Name: \_\_\_\_\_

## Worksheet 6 - Section 15.4, 15.7 (Due Tues, Nov. 4)

Math 2110Q – Fall 2014

Professor Hohn

You must show all of your work to receive full credit!

1. Use a double integral to find the area of the region inside the cardioid  $r = 1 + \cos \theta$  and outside the circle  $r = 3 \cos \theta$ .

2. Evaluate the integral

$$\int_0^2 \int_0^{\sqrt{2x-x^2}} \sqrt{x^2 + y^2} \, dy \, dx$$

by converting to polar coordinates.

3. We define the improper integral (over the entire plane  $\mathbb{R}^2$ )

$$\iint_{\mathbb{R}^2} e^{-(x^2+y^2)} dA = \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} e^{-(x^2+y^2)} dA = \lim_{a \rightarrow \infty} \iint_{D_a} e^{-(x^2+y^2)} dA$$

where  $D_a$  is the disk with radius  $a$  and center at the origin. Show that

$$\int_{-\infty}^{\infty} \int_{-\infty}^{\infty} e^{-(x^2+y^2)} dA = \pi.$$

4. Evaluate the triple integral

$$\iiint_E xy \, dV$$

where  $E$  is bounded by the parabolic cylinders  $y = x^2$  and  $x = y^2$  and the planes  $z = 0$  and  $z = x + y$ .