Score: _____

WORKSHEET 7 - DUE 11/2

MATH 2110Q – Fall 2015 Professor Hohn

You must show all of your work for full credit. Please circle/box your answers or write a brief sentence indicating your answer.

- 1. Your favorite visitor from planet Zorg returns and tells you that the following equalities are all true. Should you believe the visitor? Why or why not?
 - (a)

$$\int_{-1}^{2} \int_{0}^{6} x^{2} \sin(x-y) \, dx \, dy = \int_{0}^{6} \int_{-1}^{2} x^{2} \sin(x-y) \, dx \, dy$$

(b)
$$\int_0^1 \int_0^x \sqrt{x+y^2} \, dy \, dx = \int_0^x \int_0^1 \sqrt{x+y^2} \, dx \, dy$$

$$\int_{1}^{2} \int_{3}^{4} x^{2} e^{y} \, dy \, dx = \int_{1}^{2} x^{2} \, dx \int_{3}^{4} e^{y} \, dy$$

2. Find the volume of the solid enclosed by the paraboloid $z = x^2 + 3y^2$ and the planes x = 0, y = 1, y = x, z = 0.

3. Evaluate the integral

$$\int_0^4 \int_{\sqrt{x}}^2 \frac{1}{y^3 + 1} \, dy \, dx$$

4. In evaluating a double integral over a region D, a sum of integrals was obtained as follows:

$$\iint_{D} f(x,y) \, dA = \int_{0}^{1} \int_{0}^{2y} f(x,y) \, dx \, dy + \int_{1}^{3} \int_{0}^{3-y} f(x,y) \, dx \, dy.$$

Sketch the region D and express the double integral as an integral with reversed order of integration.