- 1. <, >,or =.
 - (a) $\tan(100^{\circ})$ $\tan(1^{\circ})$
 - (b) The solution x of $\log_{\sqrt{8}} x = \frac{8}{3}$ 10
 - (c) The period of the function $f(x) = 3\sin(\pi x 5) + 7$ The amplitude of the function $f(x) = 3\sin(\pi x 5) + 7$
 - (d) $3 \log_2 3$ $2 \log_5 6$
 - (e) The period of $f(x) = 4\tan(3x)$ The period of $g(x) = 4\cos(3x)$

2. Find all solutions to $\sin(2x) + \cos x = 0$ on the interval $[0, 2\pi)$.

- 3. Give an example of a function that is neither even nor odd, and explain why it is neither.
- 4. Find the first term of a geometric sequence whose second term is 8 and whose fifth term is 27.

5. Where is the function $f(x) = \frac{\sqrt{\sin x}}{x^2 - 4x + 3}$ defined on the interval $[0, 2\pi]$? Write your answer as a union of intervals.

- 6. Find the fifth term of the recursive sequence defined by the equations $a_1 = 2$ and $a_{n+1} = \frac{1}{a_n + 1}$.
- 7. Find an exact expression for $\sin(75^\circ)$.
- 8. Find all real numbers x such that $12x^4 + 5x^2 2 = 0$.
- 9. Find the domain and range of $f(x) = \log(-x)$. What is the inverse function of f(x)? Find the domain and range of the inverse function of f(x).
- 10. Prove the following identity

$$\sin\theta\cos\theta = \frac{\tan\theta}{1+\tan^2\theta}\,.$$

- 11. Find the linear function, y = mx + b, that passes through the vertices of $y = x^2 + 4x$ and $y = 2(x + 1)^2$.
- 12. A population of 8 frogs increases at an annual rate of 50% a year. How many frogs will there be in 4 years?
- 13. Suppose $\sin u = \frac{3}{7}$. Evaluate $\cos(2u)$.
- 14. Suppose $9^x = 4$. Evaluate $(\frac{1}{27})^{2x}$.
- 15. The function f is defined by f(-3) = 8, f(1) = 4, and f(4) = -8. Make a table for g(x) where g(x) = 2f(-5x+1) 3.
- 16. What is $\sin^{-1}(\sin(\frac{3\pi}{4}))$?
- 17. Find a number t such that the equation $x^2 + 8x + t = 0$ has exactly one solution.
- 18. What is the minimum value of the function f defined by $f(x) = 9x^2 + 30x + 18$?
- 19. Find an exact expression for $\sin(\frac{\pi}{16})$.

20. Evaluate
$$\sum_{j=1}^{22} (-5)^j$$
.

- 21. Write $2^8 \frac{4}{16^{28}}$ as a power of 4.
- 22. Find the smallest possible positive number x such that $16\sin^4 x 16\sin^2 x + 3 = 0$.
- 23. Let $f(x) = \frac{x^4 2x^2 35}{2x^4 8}$. Find the vertical and horizontal asymptotes of f(x). What are the zeros of f? 24. Write $\frac{3+5i}{(1-3i)^2}$ in a+bi form.
- 25. Give an example of an odd function whose domain is the real numbers and whose range is $\{-\pi^2, 0, \pi^2\}$.
- 26. Calculate $\log(\frac{1}{2}) + \log(\frac{2}{3}) + \dots + \log(\frac{99}{100})$.

- 27. High tide at La Jolla Cove occurs at 5 am and is 6.5 ft. Low tide occurs at 11 am and is -0.5 ft. A simple model for such tides could be a cosine function of the form $f(x) = a\cos(bx + c) + d$. Determine the values for a > 0, b, c, and d for f(x) where x represents the number of hours since midnight. Sketch f(x).
- 28. Evaluate $1 \frac{1}{2} + \frac{1}{4} \frac{1}{8} + \dots + \frac{1}{2^{80}} \frac{1}{2^{81}}$.
- 29. Evaluate $\cos(\tan^{-1} 5)$.
- 30. Write the series explicitly and evaluate the sum of $\sum_{k=0}^{3} \log(k^2 + 2)$.
- 31. Convert the polar coordinates given to rectangular coordinates in the xy-plane.

(a)
$$r = 4, \ \theta = 101\pi$$

(b) $r = 6\pi, \ \theta = \frac{11\pi}{4}$

- 32. Find the first term of a geometric sequence whose second term is 6 and whose fifth term is 162.
- 33. Simplify each of the following expressions.
 - (a) $\sin^{-1}(\cos(\frac{5\pi}{6}))$
 - (b) $\sin(\cos^{-1} x)$
- 34. Solve for x in the following equations.
 - (a) $\log_4 x + \log_4 (x 3) = 1$
 - (b) $e^x + 2e^{-x} = 3$
- 35. Each year the local country club sponsors a tennis tournamennt. Play starts with 128 participants. During each round, half of the players are eliminated. How many players remain after 5 rounds?
- 36. Show that $\sin^2(2x) = 4(\sin^2 x \sin^4 x)$.
- 37. Compute the sum of the first 20 terms of the sequence whose n^{th} term is given by $a_n = 3 + 2(n-1)$.
- 38. Sketch the graph of the function $4\sin(2x+1) + 5$ on the interval $[-3\pi, 3\pi]$.

39. Let
$$f(x) = \frac{6x+1}{5x-9}$$
.

- (a) Find the domain of f.
- (b) Find the range of f.
- (c) Find a formula for f^{-1} .
- (d) Find the domain of f^{-1} .
- (e) Find the range of f^{-1} .

40. Evaluate $\sum_{m=2}^{\infty} \frac{5}{6^m}$.

41. Simplify the expression $\left(\frac{(3t^9w^{-5})^4}{(t^{-3}w^7)^5}\right)^{-2}$.

42. Suppose you go to the fair and decide to ride the Ferris Wheel. The Ferris Wheel has a 30 meter diameter and turns 3 revolutions per minute with its lowest point 1 meter off the ground. Assume your height h above the ground is a function of the form $h(x) = a \cos(bx + c) + d$, where x = 0 represents the lowest point on the wheel and x is measured in seconds. Find the values of a > 0, b > 0, c, and d, and sketch h(x).

43. Show that
$$2 - \log x = \log\left(\frac{100}{x}\right)$$
 for every positive x.

- 44. About how many years does it take for \$600 to become \$1800 when compounded continuously at 8% per year?
- 45. Suppose $\frac{\pi}{2} < \theta < \pi$ and $\tan \theta = -4$. Evaluate
 - (a) $\cos\theta$
 - (b) $\sin \theta$

- 46. Find exact values for the following
 - (a) $\sin(-\frac{3\pi}{2})$
 - (b) $\cos \frac{15\pi}{4}$
 - (c) $\cos 360045^{\circ}$
 - (d) $\sin 300^{\circ}$
- 47. Use the figure to the right to solve the following:

Suppose a = 3 and c = 8. Evaluate

- (a) $\cos v$
- (b) $\sin v$
- (c) $\tan v$
- 48. Evaluate $\cos(\cos^{-1}\frac{2}{5})$.
- 49. Find a number b such that $\cos x + \sin x = b \sin(x + \frac{\pi}{4})$.



51. For $f(x) = \frac{x-1}{x^2+1}$ and $g(x) = \frac{x+3}{x+4}$, find the formulas for (a) $f \circ g$ (b) $g \circ f$

Simplify your results as much as possible.

- 52. Suppose $g(x) = x^7 + x^3$. Evaluate $(g^{-1}(4))^7 + (g^{-1}(4))^3 + 4$.
- 53. Evaluate the expression $\sin\left[\sec^{-1}\left(\frac{5}{3}\right) + \tan^{-1}\left(\frac{3}{4}\right)\right]$.
- 54. Find the 100^{th} term of an arithmetic sequence whose tenth term is 5 and whose eleventh term is 8.
- 55. Use the figure to the right to solve the following:

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Suppose b = 3 and \sin v = \frac{1}{3}.
Evaluate a.
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56. Evaluate $\lim_{n \to \infty} \frac{4n^2 + 1}{3n^2 - 5n}$.

57. Let g(x) be of the form $g(x) = a\cos(bx + c) + d$. Find the values for a, b, c, and d with a > 0, b > 0, and $0 \le c \le \pi$ so that g has range [-3, 4], g(0) = 2, and g has period 5.



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